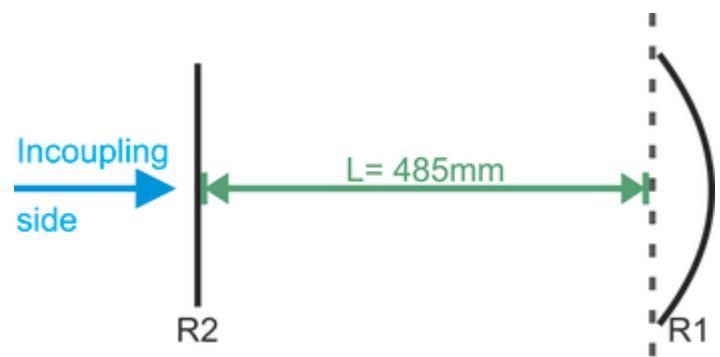


# Mode matching

## Literature



- Laser Beams and Resonators

H. Kogelnik et al., Applied Optics **5**, 1550 (1966)

## Mirror configuration

### Parameter

- Radius of curvature of mirror R1:  $R_1 = 1 \text{ m}$
- Radius of curvature of mirror R2:  $R_2 = \infty$  (Incoupling side)
- Wavelength:  $\lambda = 1.55 \times 10^{-6} \text{ m}$
- Length between the resonator mirrors:  $L = 485 \text{ mm}$
- Beam radius at waist:  $w_0$
- Beam radius at mirror:  $w_1, w_2$
- Stability parameter of the resonator:  $g_1, g_2$
- Distance between mirror and the waist:  $t_1, t_2$

## Beam waist calculation from resonator

### Step 1:

$$g_1 = 1 - \frac{L}{R_1} \quad \text{and} \quad g_2 = 1 - \frac{L}{R_2}$$

### Step 2:

From thesis of Sana:

- Beam Radii,  $1/e^2$  of the intensity

$$\begin{aligned} w_1 &= \sqrt{L \cdot \frac{\lambda}{\pi}} \cdot \left( \frac{g_2}{g_1} + \frac{g_1}{g_2} - 2 \right)^{1/4} \\ w_2 &= \sqrt{L \cdot \frac{\lambda}{\pi}} \cdot \left( \frac{g_1}{g_2} + \frac{g_2}{g_1} - 2 \right)^{1/4} \end{aligned}$$

Alternative from Appl. Opt. 5, 1550 (1966):

$$w_1 = \sqrt{\frac{\lambda}{\pi} \cdot R_1} \cdot \left( \frac{(R_2 - L) \cdot L}{(R_1 - L) \cdot (R_1 + R_2 - L)} \right)^{1/4}$$

$$w_2 = \sqrt{\frac{\lambda}{\pi} \cdot R_2} \cdot \left( \frac{(R_1 - L) \cdot L}{(R_2 - L) \cdot (R_1 + R_2 - L)} \right)^{1/4}$$

$$w_0 = \sqrt{\frac{\lambda}{\pi}} \cdot \left( \frac{L}{R_1} \right)^{1/2}$$

$L \cdot (R_2 - L) \cdot (R_1 + R_2 - L) \cdot ((R_1 + R_2 - 2L)^2) \cdot \right)^{1/4}$  In our case:

$\$w_2=w_0$  **Step 3**

Position of the beam waist from the two mirrors:

$\$t_1 = L \cdot \frac{R_2 - L}{R_1 + R_2 - 2L}$   $\$t_2 = L \cdot \frac{R_1 - L}{R_1 + R_2 - 2L}$

In our case:  $L=t_1+t_2$  **Step 4**

Take the radii on the plane  $w_2=w_0=496.567\mu m$  and curve mirror  $w_1=691.95\mu m$  and calculate the focal length f:  $f=D \cdot \left( \frac{\pi w}{4\lambda} \right)$  D is the beam waist diameter of the collimated beam after the collimator and w is mode beam diameter of the fiber output. In our case is w:  $w=2*w_0$

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